## ISLAMIC UNIVERSITY OF TECHNOLOGY (IUT) <br> ORGANISATION OF ISLAMIC COOPERATION (OIC)

## DEPARTMENT OF BUSINESS AND TECHNOLOGY MANAGEMENT

Mid-Semester Examination
Course No. : Math 4101
Course Title : Mathematics I

Winter Semester, A. Y. 2022-2023
Time $\quad: 1.5$ hours
Full Marks : 75

Answer all 3 (three) questions. All questions carry equal marks. Marks of each question and corresponding CO and PO are written in the right margin with brackets.

1. a) Solve the following inequality and show the results on the real axis $\frac{3}{|2 x-1|} \geq 4$.
b) Solve the following Non-linear inequality and show the results on the real axis.

7 (COI)

$$
\begin{equation*}
x^{2}-x-12<0 \tag{PO1}
\end{equation*}
$$

c) In a class of 25 students, 12 students have taken economics, 8 have taken economics but not politics. Find the number of students who have taken economics and politics (PO1) and those who have taken politics but not economics
2. a) Reduce the equation $2 x^{2}-10 x y+2 y^{2}+11 x-5 y+2=0$ to one containing only the terms of $2^{\text {nd }}$ degree.
b) Determine the equation of the curve. $x^{2}-2 x y+y^{2}+2 x-4 y+3=0$, after rotating the 7 (CO2) axis through $45^{\prime \prime}$.
c) If the pair of Straight lines $x^{2}-2 p x y-y^{2}=0$ and $x^{2}-2 q x y-y^{2}=0$ be such that each pair bisects the angle between the other pair, then prove that, $p-q=0$ and $p q=-1$
3. Does $x^{2}+6 x y+9 y^{2}+4 x+12 y-5=0$ represent a pair of straight lines? If yes, find and sketch them. Also find the angle between them.

