



ISLAMIC UNIVERSITY OF TECHNOLOGY (IUT)  
ORGANISATION OF ISLAMIC COOPERATION (OIC)

**DEPARTMENT OF BUSINESS AND TECHNOLOGY MANAGEMENT**

Semester Final Examination

Winter Semester, A. Y. 2022-2023

Course No. : Math 4361

Time : 3 hours

Course Title : Mathematics II

Full Marks : 150

Answer **all 6 (six)** questions. All questions carry equal marks. Marks of each question and corresponding CO and PO are written in the right margin with brackets.

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|----|--|------|----------------|
| 1. | a) Evaluate the indefinite integral $\int e^x \sin x \, dx$ through repeated integration by parts.   | 09   | (CO3)<br>(PO2) |
|    | b) Evaluate the integrals: (i) $\int x^2 \sqrt{x-1} \, dx$ (ii) $\int_1^2 \left( \frac{1}{x} + \sqrt{9-x^2} \right) dx$  | 08   | (CO3)<br>(PO2) |
|    | c) Sketch the region whose area is represented by the definite integral $\int_0^4 \sqrt{16-x^2} \, dx$ , and evaluate the integral using an appropriate formula from geometry. Also find the area by using calculus. | 08   | (CO3)<br>(PO2) |
| 2. | a) Solve the initial (boundary) value problem $\frac{dy}{dt} = \frac{3}{\sqrt{1-t^2}}$ ; $y\left(\frac{\sqrt{3}}{2}\right) = 0$ .  | 12.5 | (CO3)<br>(PO3) |
|    | b) Verify Mean Value theorem (MVT) for $f(x) = \sqrt{49-x^2}$ in the interval $[-7, 3]$ .  | 12.5 | (CO3)<br>(PO4) |
| 3. | a) Find the area of the region enclosed by $x = 2 - y^2$ and $y = -x$ .  | 12.5 | (CO3)<br>(PO4) |
|    | b) Find the total area between the curve $y = 1 - x^2$ and the x-axis for the interval $[0, 2]$ .  | 12.5 | (CO3)<br>(PO4) |
| 4. | a) Discuss the fixed-point iteration method for finding a real root of the equation $f(x) = 0$ . Use this method to find a real root of $f(x) = x^3 + x^2 - 1 = 0$ correct up to 2-decimal points.                   | 12.5 | (CO4)<br>(PO4) |
|    | b) Discuss the Newton-Raphson's method for finding a real root of the equation $f(x) = 0$ . Use this method to find a real root of $f(x) = e^x - x^2 + 3x - 2 = 0$ in $[0, 1]$ correct upto 2-decimal places.        | 12.5 | (CO4)<br>(PO4) |
| 5. | Given points $(x, f(x))$ as $(1, 1), (2, 8), (3, 27), (4, 64), (5, 125), (6, 216), (7, 343)$ and $(8, 512)$ .  | 25   | (CO3)<br>(PO4) |
|    | (i) Use Newton's Forward difference interpolation formula to find $f(2.5)$ .   |      |                |
|    | (ii) Use Newton's Backward difference interpolation formula to find $f(7.5)$ .   |      |                |

6. a) Derive Euler's Method for solving 1<sup>st</sup> order differential equation. Use this method to solve  $\frac{dy}{dx} = x + y$ ,  $y(0) = 1$  at  $x = 0.05$ ,  $x = 0.1$  taking  $h = 0.05$ . 12.5 (CO4) (PO5)
- b) Derive 2<sup>nd</sup> order Runge-Kutta Method for solving 1<sup>st</sup> order ordinary differential equation. Use this method to find  $y(0.4)$  from the IVP  $5 \frac{dy}{dx} = x^2 + y^2$ ,  $y(0) = 0$  and  $h = 0.2$ . 12.5 (CO4) (PO5)